**Highlights**

- Complex models of chromosome evolution fit better in Cyperaceae megaphylogeny

- Three transitions in the model of chromosome number evolution in sedges

- Chromosome number evolution may explain shifts in diversification rates in sedges